國立中央大學九十二學年度碩士班考試入學招生試題卷

共2頁第1頁

系所別:

機械工程學系 丁絲

丁組 科目:

自動控制

1. The open-loop transfer function of a unity feedback system is

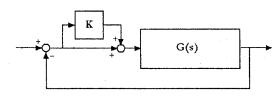
$$G(s) = \frac{K}{s(s+2)}$$

The desired system response to a step input is specified as peak time $t_p=1$ sec and Overshoot $M_p=5\%$.

- (a) Determine where both specifications can be met simultaneously by selecting the right value of K. (15%)
- (b) Sketch the associated region in the s-plane where both specifications are met. (5%)



2. 一閉迴路系統如下圖 (Fig. 1) 所示,



其中

$$G(s) = \frac{10}{2s^3 + 11s^2 + 17s + 6}$$

- (a) 請劃出 G(s)的 Nyquist Plot,並標示出它與實數軸與虛數軸的交點(15%)。
- (b) 請問當 K=2 與 8 時, KG(jω)與實數軸的交點為何? (ω代表頻率)(5%)
- (c) 就(b)所得之交點, 說明當 K=2 與 8 時閉迴路是否為穩定的系統(5%)。
- (d) 依據你所劃的 Nyquist Plot 找出使得上圖閉迴路穩定的 K 的範圍(5%)。

國立中央大學九十二學年度碩士班考試入學招生試題卷 共2頁 第2頁

機械工程學系 丁組 科目:

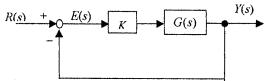
3. The open loop system with the transfer function is

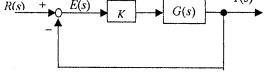
$$G(s) = \frac{1}{(s+1)(s^2+100)}$$

If the sinusoidal input signal $u(t) = 10\cos(100t)$ over the interval $0 \le t \le 10$ sec., assuming zero initial conditions.

- (a) Compute the sinusoidal steady-state response $y_{ss}(t)$. (4%)
- (b) Draw u(t) & $y_{ss}(t)$ in a single plot, and comment on their relationships to one another. (4%)

Now, if the proportional control system is shown as the following figure.





- (c) Draw the Bode plot for K = 1. (4%)
- (d) Find the phase margin and gain margin of (c). Is the system stable? (4%)
- (e) Determine the approximate range of K such that the control system is stable from (c). (4%)
- 4. Answer the following questions.
- (a) In an s-plane, indicate poles that have the same envelope. (5%)
- (b) Given Fig 1, to improve steady-state response only, an integrator is added in the forward path and this causes an extra pole at the origin, creating a new root locus. But in fact, the transient response was not affect appreciably. Why? (10%)
- (c) Given a compensator G_c=(s+z_c)/(s+p_c), how do you differentiate a lead compensator from a lag compensator in terms of z_e and p_e. (10%)
- (d) Root locus technique is based on two criterions. Please describe them. (5%)

